

# Package ‘EMMIXuskew’

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**Type** Package

**Title** Fitting Unrestricted Multivariate Skew t Mixture Models

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**Description** Functions to fit finite mixture of unrestricted multivariate skew t (FM-uMST) model, random sample generation, discriminant analysis, 2D and 3D contour plots

**License** GPL

**LazyLoad** yes

**Suggests** rgl, stats, grDevices, KernSmooth

**Depends** MASS, graphics

**Archs** i386, x64

## R topics documented:

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EMMIXuskew-package	<i>Finite mixture of unrestricted multivariate skew t distributions</i>
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## Description

This package implements an EM algorithm for fitting mixtures of unrestricted multivariate skew t (FM-uMST) distributions. Functions for random sample generation, discriminant analysis, and visualisation (in 2D and 3D) is also provided.

## Details

Package:	EMMIXuskew
Type:	Package
Version:	0.11-6
Date:	2014-07-31
Licence:	GPL
LazyLoad:	yes

## Author(s)

S.X. Lee, G.J. McLachlan

## References

- Lee S, McLachlan G (2011). On the fitting of mixtures of multivariate skew t-distributions via the EM algorithm. arXiv:1109.4706 [stat.ME]
- Lee, S. and McLachlan, G.J. (2014) Finite mixtures of multivariate skew t-distributions: some recent and new results. *Statistics and Computing*, 24, 181-202.
- Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## See Also

[fmmst](#), [dfmmst](#), [rfmmst](#), [fmmst.contour.3d](#)

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ais	<i>Australian Institute of Sports (AIS) data</i>
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## Description

Data on 102 male and 100 female athletes collected at the Australian Institute of Sport.

## Usage

```
data(ais)
```

**Format**

A data frame with 202 observations (rows) on the following 14 variables (columns).

Sex 0 = male or 1 = female

Ht Height in cm

Wt Weight in kg

LBM Lean body mass

RCC Red cell count

WCC White cell count

Hc Hematpcrit

Hg Hematocrit

Ferr Plasma ferritin concentration

BMI Body mass index =  $\text{weight} / (\text{height}^2)$

SSF sum of skin folds

Bfat Percent body fat

Label case labels: f-b\_ball f-field f-gym f-netball f-row f-swim f-t\_400m f-t\_sprnt  
f-tennis m-b\_ball m-field m-row m-swim m-t\_400m m-t\_sprnt m-tennis m-w\_polo

Sport Sport: b\_ball field gym netball row swim t\_400m t\_sprnt tennis w\_polo

**Source**

Richard Telford and Ross Cunningham, Australian National University.

**References**

S. Weisberg (2005). Applied Linear Regression, 3rd edition. New York: Wiley, Section 6.4

**Examples**

```
data(ais)
pairs(ais[,2:12], main = "AIS Data", pch = 21,
      bg = c("red", "blue")[unclass(factor(ais$Sex))], upper.panel=NULL)
legend(0.8, 0.8, legend=c("male", "female"), pt.bg = c("red", "blue"), pch=21)
```

---

delta.test

*Testing for the significance of the skewness parameter in a FM-MST model*

---

**Description**

Perform a likelihood ratio for the significance of the skewness parameter delta in a multivariate skew t-mixture model.

**Usage**

```
delta.test(stmodel=NULL, tmodel=NULL, stloglik, tloglik, r)
```

### Arguments

stmodel	a list containing the parameters of the FM-MST model, including mu, sigma, delta, dof and pro. This is usually an output from a fmmst run.
tmodel	a list containing the parameters of the FM-MT model, including mu, sigma, dof and pro. This is usually an output from a fmmt run.
stloglik	a scalar specifying the log likelihood value of the skew t-mixture model
tloglik	a scalar specifying the log likelihood value of the t-mixture model
r	a scalar specifying the difference in the number of parameters between FM-MST and FM-MT model

### Details

A likelihood ratio test for hypotheses:

H0:  $\delta = 0$  (for all components in the mixture model)

H1:  $\delta$  different from 0 (for at least one component in the mixture)

The test statistics is  $LR = -2 (L1 - L2)$ , which follows a chi-squared distribution with  $r$  degrees of freedom under H0.  $r$  is the difference between the number of parameters in H0 and H1. See references for further details.

### Value

returns the P-value of the test

### References

Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. Journal of Statistical Software, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

### See Also

[fmmst](#), [fmmt](#)

### Examples

```
delta.test(stloglik=-1343.541, tloglik=-1353.842, r=4)
```

---

dfmmst

---

*Multivariate skew t distribution*


---

### Description

The probability density function for the unrestricted multivariate skew t (MST) distribution and finite mixture of MSN and MST distributions

### Usage

```
dfmmst(dat, mu = NULL, sigma = NULL, delta = NULL, dof = NULL, pro = NULL,
        known = NULL, tmethod=1)
dmst(dat, mu = NULL, sigma = NULL, delta = NULL, dof = 1, known = NULL, tmethod=1)
```

## Arguments

<code>dat</code>	the data matrix giving the coordinates of the point(s) where the density is evaluated. This is either a vector of length $p$ or a matrix with $p$ columns.
<code>mu</code>	for <code>dmst</code> , this is a numeric vector of length $p$ representing the location parameter; for <code>dfmmst</code> , this is list of $g$ numeric matrices each having $p$ rows and 1 column containing the location parameter for each component.
<code>sigma</code>	for <code>dmst</code> , this is a numeric positive definite matrix with dimension $(p, p)$ representing the scale parameter; for <code>dfmmst</code> , this is list of $g$ numeric matrices containing the scale parameter for each component.
<code>delta</code>	for <code>dmst</code> , this is a numeric vector of length $p$ representing the skewness parameter; for <code>dfmmst</code> , this is list of $g$ numeric matrices each having $p$ rows and 1 column containing the skewness parameter for each component.
<code>dof</code>	for <code>dmst</code> , this is a positive integer specifying the degrees of freedom; for <code>dfmmst</code> , this is numeric vector of length $g$ representing the degrees of freedom for each component.
<code>pro</code>	the mixing proportions; for <code>dmst</code> , this is equal to 1; for <code>dfmmst</code> , this is vector of length of $g$ specifying the mixing proportions for each component.
<code>known</code>	a list containing the parameters of the model. If specified, it overwrites the values of <code>mu</code> , <code>sigma</code> , <code>delta</code> , <code>dof</code> and <code>pro</code> .
<code>tmethod</code>	(optional) an integer indicating which method to use when computing $t$ distribution function values. See <a href="#">pmt</a> for details.

## Details

The function `dmst` computes the density value of a specified unrestricted multivariate skew  $t$  (MST) distribution. If any model parameters are not specified, their default values are used: `mu` and `delta` are zero vectors, `sigma` is the identity matrix, and `dof` is 1.

The function `dfmmst` computes the density value for a specified mixture of MST distribution. Note that `dfmmst` expects at least `dof` is specified. Other missing parameters will take the default value described above. When  $g=1$ , `dfmmst` passes the call to `dmst`. Model parameters can be passed to `dmst` and `dfmmst` through the argument `known` or listed as individual arguments. If both methods of input were used, the parameters specified in `known` will be used.

## Value

`dmst` and `dfmmst` returns a numeric vector of density values

## References

- Sahu S, Dey D, Branco M (2003). A New Class of Multivariate Skew Distributions with Applications to Bayesian Regression Models. *The Canadian Journal of Statistics*, 31, 129-150.
- Lee S, McLachlan G (2011). On the fitting of mixtures of multivariate skew  $t$ -distributions via the EM algorithm. [arXiv:1109.4706 \[stat.ME\]](#)
- Lee, S. and McLachlan, G.J. (2014) Finite mixtures of multivariate skew  $t$ -distributions: some recent and new results. *Statistics and Computing*, 24, 181-202.

## See Also

[rmst](#), [rfmmst](#)

## Examples

```
dmst(c(1,2), mu=c(1,5), sigma=diag(2), delta=c(-3,1), dof=4)
obj <- list()
obj$mu <- list(c(17,19), c(5,22), c(6,10))
obj$sigma <- list(diag(2), matrix(c(2,0,0,1),2), matrix(c(3,7,7,24),2))
obj$delta <- list(c(3,1.5), c(5,10), c(2,0))
obj$dof <- c(1, 2, 3)
obj$pro <- c(0.25, 0.25, 0.5)
dfmmst(matrix(c(1,2,5,6,2,4),3,2), obj$mu, obj$sigma, obj$delta,
  obj$dof, obj$pro)
dfmmst(c(1,2), known=obj)
```

---

DLBCL

*A Diffuse Large B-cell Lymphoma (DLBCL) data*


---

## Description

A sample from the Diffuse Large B-cell Lymphoma (DLBCL) dataset from Aghaeepour et al. (2013). The original data contain measurements from biopsies of 30 DLBCL patients. Each sample was stained with three antibodies, CD3, CD5, and CD19. This is a subset from one patient.

## Usage

```
data(DLBCL)
```

## Format

DLBCL is a data frame with over 8000 observations (rows) on the following 3 markers (rows).

CD3 marker 1

CD5 marker 2

CD19 marker 3

## Details

DLBCL is a data frame as described above. `true.clusters` is a set of cluster labels given by manual gating.

## Source

The raw data is available from the FlowRepository database. <https://flowrepository.org/id/FR-FCM-ZZYY>

## References

- Spidlen J, Breuer K, Rosenberg C, Kotecha N and Brinkman RR. (2012) FlowRepository - A Resource of Annotated Flow Cytometry Datasets Associated with Peer-reviewed Publications. *Cytometry A*, 81(9):727-31.
- Aghaeepour et al. (2013) Critical assessment of automated flow cytometry analysis techniques. *Nature Methods*, 10, 228-238.
- Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## Examples

```
data(DLBCL)
## Not run:
RNGversion("3.0.2"); set.seed(240)
Fit <- fmmst(4, DLBCL, nkmeans=1)
fmmst.contour.3d(DLBCL, model = Fit, level = 0.985, drawpoints = FALSE,
  xlab="CD3", ylab="CD5", zlab="CD19", component=1:4)

## End(Not run)
```

---

dmt

---

*Multivariate t distribution*


---

## Description

The probability density function and distribution function for the multivariate Student t distribution and mixtures of multivariate t distribution

## Usage

```
dmt(dat, mu, sigma, dof = Inf, log = FALSE)
pmt(dat, mu=rep(0,length(dat)), sigma=diag(length(dat)), dof=Inf, method=1, ...)
dfmmt(dat, mu = NULL, sigma = NULL, dof = NULL, pro = NULL, known = NULL)
```

## Arguments

dat	for dmt, this is the data matrix giving the coordinates of the point(s) where the density is evaluated. for pmt, this is either a vector of length p. Currently, only p up to 20 dimensions is supported.
mu	a numeric vector of length p representing the location parameter;
sigma	a numeric positive definite matrix with dimension (p,p) representing the scale parameter
dof	a positive real number specifying the degrees of freedom. If tmethod=1, dof will be rounded to the nearest integer.
pro	the mixing proportions; for dmt, this is equal to 1; for dfmmt, this is vector of length of g specifying the mixing proportions for each component.
log	a logical value; if TRUE, the logarithm of the density is computed
...	parameters passed to sadmvt, among maxpts, absrel, releps

known	a list containing the parameters of the model. If specified, it overwrites the values of mu, sigma, dof and pro.
method	the method to use for computation of t distribution function. See description.

## Details

There are three options in pmt for computing multivariate t distribution function values. method=1 uses requires dof to be an integer. This provide interfaces to the Fortran-77 routines by Alan Genz. This is the fastest method of the three options available. method=2 uses linear interpolation technique to calculate t distribution function values for a positive real dof. This method requires double the time of method 1. method=3 uses a method described in Genz and Bretz (2002). This is the more accurate method for a non-integer dof, but more computationally intensive than the other two methods.

## Value

The function dmt computes the density value of a specified multivariate t distribution. pmt computes the distribution value for a SINGLE point. dfmmt returns a numeric vector of mixture density values.

## References

Genz, A.: Fortran code in files mv.t.f and mvtdstpack.f available at <http://www.math.wsu.edu/math/faculty/genz/software/>

Genz, A. and Bretz, F. (2002). Comparison of Methods for the Numerical Computation of Multivariate t Probabilities. J. of Comput. Graph. Stat., 11:950-971,

## See Also

[dmst](#), [dfmmt](#)

## Examples

```
x <- seq(-2,4,length=21)
y <- 2*x+10
z <- x+cos(y)
mu <- c(1,12,2)
sigma <- matrix(c(1,2,0,2,5,0.5,0,0.5,3), 3, 3)
dof <- 4
f <- dmt(cbind(x,y,z), mu, sigma,dof)
## Not run:
p1 <- pmt(c(2,11,3), mu, sigma, dof)
p2 <- pmt(c(2,11,3), mu, sigma, dof, maxpts=10000, abseps=1e-8)

## End(Not run)

obj <- list()
obj$mu <- list(c(17,19), c(5,22), c(6,10))
obj$sigma <- list(diag(2), matrix(c(2,0,0,1),2), matrix(c(3,7,7,24),2))
obj$dof <- c(1, 2, 3)
obj$pro <- c(0.25, 0.25, 0.5)
dfmmt(matrix(c(1,2,5,6,2,4),3,2), obj$mu, obj$sigma, obj$dof, obj$pro)
dfmmt(c(1,2), known=obj)
```



fmmst

---

*Fitting Finite Mixtures of Unrestricted Multivariate Skew  $t$  Distributions*


---

## Description

Computes maximum likelihood estimators (MLE) for finite mixtures of unrestricted multivariate skew  $t$  (FM-MST) model via the EM algorithm.

## Usage

```
fmmst(g = 1, dat, initial = NULL, known = NULL, itmax = 100,
      eps = 1e-03, clust=NULL, nkmeans=20, print = T, tmethod=1)
## S3 method for class 'fmmst'
summary(object, ...)
## S3 method for class 'fmmst'
print(x, ...)
```

## Arguments

object, x	an object class of class "fmmst", i.e. a fitted model.
g	a scalar specifying the number of components in the mixture model
dat	the data matrix giving the coordinates of the point(s) where the density is evaluated. This is either a vector of length $p$ or a matrix with $p$ columns.
initial	(optional) a list containing the initial parameters of the mixture model. See the 'Details' section. The default is NULL.
known	(optional) a list containing parameters of the mixture model that are known and not required to be estimated. See the 'Details' section. The default is NULL.
itmax	(optional) a positive integer specifying the maximum number of EM iterations to perform. The default is 100.
eps	(optional) a numeric value used to control the termination criteria for the EM loops. It is the maximum tolerance for the absolute difference between the log-likelihood value and the asymptotic log likelihood value. The default is $1e-6$ .
clust	(optional) a numeric value of length $nrow(dat)$ containing the initial labels for each data point in <code>dat</code> . The default is NULL, indicating no initial clustering is known.
nkmeans	(optional) a numeric value indicating how many k-means trials to be used when searching for initial values. The default is 20.
print	(optional) a logical value. If TRUE, output for each iteration will be printed out. if FALSE, no output is printed. The default is TRUE. See the 'Details' section.
tmethod	(optional) an integer indicating which method to use when computing $t$ distribution function values. See <a href="#">pmt</a> for details.
...	not used.

## Details

The arguments `init` and `known`, if specified, is a list structure containing at least one of `mu`, `sigma`, `delta`, `dof`, `pro` (See [dfmmst](#) for the structure of each of these elements). If `init=FALSE` (default), the program uses an automatic approach based on k-means clustering to generate an initial value for the model parameters. Note that this may not provide the best results.

As the EM algorithm is sensitive to the starting value, it is highly recommended to apply a wide range different initializations. A simple strategy is implemented in [fmmst.init](#).

## Value

<code>mu</code>	a list of <code>g</code> numeric matrices containing the location parameter for each component.
<code>sigma</code>	a list of <code>g</code> numeric matrices containing the scale parameter for each component.
<code>delta</code>	a list of <code>g</code> numeric matrices containing the skewness parameter for each component.
<code>dof</code>	a numeric vector of length <code>g</code> representing the degrees of freedom for each component.
<code>pro</code>	a vector of length of <code>g</code> specifying the mixing proportions for each component.
<code>tau</code>	an <code>g</code> by <code>n</code> matrix of posterior probability of component membership.
<code>clusters</code>	a vector of length <code>n</code> of final partition.
<code>loglik</code>	the final log likelihood value.
<code>lk</code>	a vector of log likelihood values at each EM iteration.
<code>iter</code>	number of iterations performed.
<code>eps</code>	the final absolute difference between the log likelihood value and the asymptotic log likelihood value.
<code>aic, bic</code>	Akaike Information Criterion (AIC), Bayes Information Criterion (BIC)

## References

- Lee S, McLachlan G (2011). On the fitting of mixtures of multivariate skew t-distributions via the EM algorithm. [arXiv:1109.4706 \[stat.ME\]](#)
- Lee, S. and McLachlan, G.J. (2014) Finite mixtures of multivariate skew t-distributions: some recent and new results. *Statistics and Computing*, 24, 181-202.
- Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## See Also

[fmmst.init](#), [rfmmst](#), [dfmmst](#), [fmmst.contour.2d](#)

## Examples

```
#a short demo using AIS data
data(ais)
Fit <- fmmst(2, ais[,c(2,12)], itmax=5)
summary(Fit)
print(Fit)
```

## Description

Create 2D or 3D contour plot.

## Usage

```
fmmst.contour.2d(dat, model, grid = 50, drawpoints = TRUE, clusters=NULL, levels = 10,
  map = c("scatter", "heat", "cluster"), component = NULL,
  xlim, ylim, xlab, ylab, main, tmethod=1, ...)
fmmst.contour.3d(dat, model, grid=20, drawpoints=TRUE, levels=0.9,
  clusters=NULL, xlim, ylim, zlim, xlab, ylab, zlab, main, component=NULL, ...)
```

## Arguments

dat	the data matrix giving the coordinates of the point(s) where the density is evaluated. This must be a matrix with at least 2 columns for <code>fmmst.contour.2d</code> or 3 columns for <code>fmmst.contour.3d</code> . If <code>dat</code> is not provided, then <code>xlim</code> , <code>ylim</code> and <code>zlim</code> must be provided, and <code>drawpoints</code> must be set to <code>FALSE</code> .
model	a list containing the parameters of the model and also a vector of cluster labels for <code>dat</code> . This is typically an output from <code>fmmst</code> , containing <code>mu</code> , <code>sigma</code> , <code>delta</code> , <code>dof</code> , <code>pro</code> and <code>clusters</code> ; see <code>fmmst</code> for structure of <code>model</code> .
grid	a positive integer specifying the grid size used to calculate the density map.
drawpoints	logical. Points are plotted if <code>TRUE</code> .
clusters	a vector of cluster labels to be applied when colouring the points. This only applies when <code>drawpoints</code> is <code>TRUE</code> .
levels	either a positive integer specifying the number of contour levels to draw or a numeric vector of contour levels to be drawn
map	character string specifying how to plot the points if <code>drawpoints=TRUE</code> . Possible values are "scatter" (default), "heat" and "cluster". See the 'Details' section.
component	the index of the components to be plotted. See the 'Details' section.
xlim, ylim, zlim	x-, y- and z- limits for the plot
xlab, ylab, zlab	labels for x-, y- and z- axis
main	title of the plot
tmethod	(optional) an integer indicating which method to use when computing t distribution function values. See <code>pmt</code> for details.
...	additional arguments to <code>plot.default</code>

## Details

`fmmst.contour.2d` draw contour plots for bivariate densities. The argument `dat` must be provided and must contain at least 2 columns. Note that only the first two columns of `dat` will be used if `dat` have more than 2 columns. For bivariate dataset, the data points can be drawn as a scatter plot by specifying `map="scatter"` (default), or as an intensity plot (`map="heat"`). Alternatively, a cluster map can be drawn instead (`map="cluster"`). Note that if an intensity plot is used, the data points will not be drawn, that is, `drawpoints` will be set to `FALSE`.

The argument `component` specifies which individual component is drawn. When `component=FALSE`, the mixture contour is drawn. If specified, `component` is a integer vector of the index of the components to be drawn. It can only take values between 1 and `g` inclusive. For example, `component=c(1,3)` will draw the first and third component contours.

If the argument `model` contains the cluster labels (`model$clusters`), the data point will be coloured according to their cluster.

## See Also

[fmmst, contour](#)

## Examples

```
#2D plots
obj <- list()
obj$mu <- list(c(17,19), c(5,22), c(6,10))
obj$sigma <- list(diag(2), matrix(c(2,0,0,1),2), matrix(c(3,7,7,24),2))
obj$delta <- list(c(3,1.5), c(5,10), c(2,0))
obj$dof <- c(1, 2, 3)
obj$pro <- c(0.25, 0.25, 0.5)
mySample <- rfmmst(3, 500, known=obj)
obj$clusters <- mySample[,3]

par(mfrow=c(2,2))
fmmst.contour.2d(mySample, model=obj, clusters=obj$clusters)
fmmst.contour.2d(mySample[,1:2], model=obj, clusters=obj$clusters, map="heat")
fmmst.contour.2d(mySample[,1:2], model=obj, clusters=obj$clusters, map="cluster")
fmmst.contour.2d(mySample[,1:2], model=obj, clusters=obj$clusters, component=1)

#3D plot
## Not run:
obj <- list()
obj$mu <- list(c(420,360,425), c(160,570,200), c(320,540,260), c(530,80,450))
obj$sigma <-
  list(matrix(c(9160,5580,7000,5580,12105,7160,7000,7160,7250),3,3),
        matrix(c(3870,1810,1770,1810,2900,1270,1770,1270,1320),3,3),
        matrix(c(1695,1190,2280,1190,2780,2010,2280,2010,3720),3,3),
        matrix(c(1590,590,15,590,2425,415,15,415,1870),3,3))
obj$delta <- list(c(4.8,-17,-50), c(-4,-80,-60), c(-40,8,-10), c(-60,90,-6))
obj$dof <- c(10,30,40,40)
obj$pro <- c(0.125, 0.19, 0.135, 0.55)
mySample <- rfmmst(4, 10000, known=obj)
obj$clusters <- mySample[,4]
fmmst.contour.3d(mySample[,1:3], model=obj, levels=0.95,
  drawpoints=F, clusters=obj$clusters, component=1:4)

## End(Not run)
```

---

fmmst.init	<i>Initialization for Fitting Finite Mixtures of Unrestricted Multivariate Skew <math>t</math> Distributions</i>
------------	--

---

## Description

Computes different sets of initial values for finite mixtures of unrestricted multivariate skew  $t$  (FM-uMST) model based on an initial clustering.

## Usage

```
fmmst.init(g, dat, known=NULL, clust=NULL, nkmeans=20, tmethod=1)
```

## Arguments

<code>g</code>	a scalar specifying the number of components in the mixture model
<code>dat</code>	the data matrix giving the coordinates of the point(s) where the density is evaluated. This is either a vector of length $p$ or a matrix with $p$ columns.
<code>known</code>	(optional) a list containing parameters of the mixture model that are known and not required to be estimated. See the 'Details' section. The default is <code>NULL</code> .
<code>clust</code>	(optional) a numeric value of length <code>nrow(dat)</code> containing the initial labels for each data point in <code>dat</code> . The default is <code>NULL</code> , indicating no initial clustering is known.
<code>nkmeans</code>	(optional) a numeric value indicating how many k-means trials to be used when searching for initial values. The default is 20.
<code>tmethod</code>	(optional) an integer indicating which method to use when computing $t$ distribution function values. See <a href="#">pmt</a> for details.

## Details

As the EM algorithm is sensitive to the starting value, it is highly recommended to apply a wide range different initializations. To obtain different sets of starting values using the strategy described in Section 5.1.3 of Lee and McLachlan (2014), `fmmst.init()` can be used, which will return a list of objects with the same structure as `initial`. An example is given in the examples section below.

The argument `known`, if specified, is a list structure containing at least one of `mu`, `sigma`, `delta`, `dof`, `pro` (See [dfmmst](#) for the structure of each of these elements). Note that although not all parameters need to be provided in `known`, the parameters that are provided must be fully specified. They cannot be partially specified, e.g. only some elements or some components are specified.

## Value

a list of initializations for `fmmst`, each containing the following parameters:

<code>mu</code>	a list of <code>g</code> numeric matrices containing the location parameter for each component.
<code>sigma</code>	a list of <code>g</code> numeric matrices containing the scale parameter for each component.
<code>delta</code>	a list of <code>g</code> numeric matrices containing the skewness parameter for each component.

dof	a numeric vector of length g representing the degrees of freedom for each component.
pro	a vector of length of g specifying the mixing proportions for each component.
tau	an g by n matrix of initial probability of component membership.
clusters	a vector of length n of initial partition.
loglik	the initial log likelihood value.

## References

- Lee S, McLachlan G (2011). On the fitting of mixtures of multivariate skew t-distributions via the EM algorithm. arXiv:1109.4706 [stat.ME]
- Lee, S. and McLachlan, G.J. (2014) Finite mixtures of multivariate skew t-distributions: some recent and new results. *Statistics and Computing*, 24, 181-202.
- Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## See Also

[rfmmst](#), [dfmmst](#), [fmmst.contour.2d](#)

## Examples

```
#a short demo using AIS data
data(ais)
Fit.init <- fmmst.init(2, ais[,c(2,12)])

#the number of available initializations
length(Fit.init)

#getting the first set of available initialization
Fit.init[[1]]
## Not run:
Fit1 <- fmmst(2, ais[,c(2,12)], initial=Fit.init[[1]])
Fit2 <- fmmst(2, ais[,c(2,12)], initial=Fit.init[[2]])

## End(Not run)
```

---

fmmstDA

*Discriminant analysis using Multivariate Skew t Mixture Models*


---

## Description

performs discriminant analysis (DA) for a specified multivariate skew t mixture distribution.

## Usage

```
fmmstDA(g, dat, model, tmethod=1)
```

## Arguments

<code>g</code>	a scalar specifying the number of components in the mixture model
<code>dat</code>	the data matrix giving the coordinates of the point(s) to be classified.
<code>model</code>	a list containing the parameters of the model, including <code>mu</code> , <code>sigma</code> , <code>delta</code> , <code>dof</code> (for <code>fmmtDA</code> only) and <code>pro</code> .
<code>tmethod</code>	(optional) an integer indicating which method to use when computing <code>t</code> distribution function values. See <a href="#">pmt</a> for details.

## Details

For the structure of the elements of `model`, see [dfmmst](#).

## Value

`fmmtDA` returns a vector of length `nrow(dat)` of the cluster labels

## references

Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew `t`-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## See Also

[dfmmst](#), [fmmt](#)

## Examples

```
obj <- list()
obj$mu <- list(c(17,19), c(5,22), c(6,10))
obj$sigma <- list(diag(2), matrix(c(2,0,0,1),2), matrix(c(3,7,7,24),2))
obj$delta <- list(c(3,1.5), c(5,10), c(2,0))
obj$dof <- c(1, 2, 3)
obj$pro <- c(0.25, 0.25, 0.5)
X2 <- rfmmst(3, 50, known=obj)
fmmtDA(3, X2[,1:2], obj)
```

---

fmmt

*Fitting Finite Mixtures of Unrestricted Multivariate t Distributions*


---

## Description

Computes maximum likelihood estimators (MLE) for finite mixtures of multivariate `t` (FM-MT) model via the EM algorithm.

## Usage

```
fmmt(g = 1, dat, initial = NULL, known = NULL, itmax = 100,
     eps = 1e-03, nkmeans=20, print = T)
## S3 method for class 'fmmt'
summary(object, ...)
## S3 method for class 'fmmt'
print(x, ...)
```

## Arguments

object, x	an object class of class "fmmt", i.e. a fitted model.
g	a scalar specifying the number of components in the mixture model
dat	the data matrix giving the coordinates of the point(s) where the density is evaluated. This is either a vector of length p or a matrix with p columns.
initial	(optional) a list containing the initial parameters of the mixture model. See the 'Details' section. The default is NULL.
known	(optional) a list containing parameters of the mixture model that are known and not required to be estimated. See the 'Details' section. The default is NULL.
itmax	(optional) a positive integer specifying the maximum number of EM iterations to perform. The default is 100.
eps	(optional) a numeric value used to control the termination criteria for the EM loops. It is the maximum tolerance for the absolute difference between the log-likelihood value and the asymptotic log likelihood value. The default is 1e-6.
nkmeans	(optional) a numeric value indicating how many k-means trials to be used when searching for initial values. The default is 20.
print	(optional) a logical value. If TRUE, output for each iteration will be printed out. if FALSE, no output is printed. The default is TRUE. See the 'Details' section.
...	not used.

## Details

The arguments `init` and `known`, if specified, is a list structure containing at least one of `mu`, `sigma`, `delta`, `dof`, `pro` (See [dfmmt](#) for the structure of each of these elements). If `init=FALSE` (default), the program uses an automatic approach based on k-means clustering to generate an initial value for the model parameters.

## Value

<code>mu</code>	a list of g numeric matrices containing the location parameter for each component.
<code>sigma</code>	a list of g numeric matrices containing the scale parameter for each component.
<code>dof</code>	a numeric vector of length g representing the degrees of freedom for each component.
<code>pro</code>	a vector of length of g specifying the mixing proportions for each component.
<code>tau</code>	an g by n matrix of posterior probability of component membership.
<code>clusters</code>	a vector of length n of final partition.
<code>loglik</code>	the final log likelihood value.
<code>lk</code>	a vector of log likelihood values at each EM iteration.
<code>iter</code>	number of iterations performed.
<code>eps</code>	the final absolute difference between the log likelihood value and the asymptotic log likelihood value.
<code>aic, bic</code>	Akaike Information Criterion (AIC), Bayes Information Criterion (BIC)



## References

- McLachlan G.J. and Krishnan T. (2008). The EM Algorithm and Extensions (2nd). New Jersey: Wiley.
- McLachlan G.J. and Peel D. (2000). Finite Mixture Models. New York: Wiley.

## See Also

[rfmmst](#), [dfmmst](#), [fmmst.contour.2d](#)

## Examples

```
#a short demo using AIS data
data(ais)
Fit <- fmmst(2, ais[,c(2,12)], itmax=10)
summary(Fit)
print(Fit)
```

---

Lympho	<i>T-cell Phosphorylation dataset</i>
--------	---------------------------------------

---

## Description

A subset of the T-cell phosphorylation dataset. The original data contain measurements of blood samples stained with four antibodies, CD4, CD45RA, SLP76 and ZAP70. Measurements from each subject were taken before and after anti-CD3 stimulation. This is a subset of the pre-stimulation data from one subject.

## Usage

```
data(Lympho)
```

## Format

A data frame with 33399 observations (rows) on the following 2 variables (columns).

```
SLP76 marker 1
ZAP70 marker 2
```

## Source

Data is available from the GenePattern website. [http://www.broadinstitute.org/cancer/software/genepattern/modules/FLAME/published\\_data](http://www.broadinstitute.org/cancer/software/genepattern/modules/FLAME/published_data).

## References

- Maier LM, Anderson DE, De Jager PL, Wicker L, Hafler DA (2007). Allelic variant in CTLA4 alters T cell phosphorylation patterns. Proceedings of the National Academy of Sciences of the United States of America, 104, 18607-18612.

## Examples

```
data(Lympho)
plot(Lympho, main="Lymphoma dataset")
smoothScatter(Lympho, nrpoints=Inf)
```

## Description

Generate random sample from a specified mixture of unrestricted multivariate skew t distribution

## Usage

```
rfmmst(g, n, mu, sigma, delta, dof = rep(10, g),
       pro = rep(1/g, g), known = NULL)
rmst(n, mu, sigma, delta, dof=1, known)
```

## Arguments

<code>g</code>	a scalar specifying the number of components in the mixture model
<code>n</code>	either a positive integer specifying the total number of points to be generated or a vector (of length <code>g</code> ) of positive integers specifying the number of points to be generated in each component.
<code>mu</code>	for <code>rmst</code> , this is a numeric vector of length <code>p</code> representing the location parameter; for <code>rfmmst</code> , this is list of <code>g</code> numeric matrices each having <code>p</code> rows and 1 column containing the location parameter for each component.
<code>sigma</code>	for <code>rmst</code> , this is a numeric positive definite matrix with dimension $(p,p)$ representing the scale parameter; for <code>rfmmst</code> , this is list of <code>g</code> numeric matrices containing the scale parameter for each component.
<code>delta</code>	for <code>rmst</code> , this is a numeric vector of length <code>p</code> representing the skewness parameter; for <code>rfmmst</code> , this is list of <code>g</code> numeric matrices each having <code>p</code> rows and 1 column containing the skewness parameter for each component.
<code>dof</code>	for <code>rmst</code> , this is a positive integer specifying the degrees of freedom; for <code>rfmmst</code> , this is numeric vector of length <code>g</code> representing the degrees of freedom for each component.
<code>pro</code>	the mixing proportions; for <code>rmst</code> , this is equal to 1; for <code>rfmmst</code> , this is vector of length of <code>g</code> specifying the mixing proportions for each component.
<code>known</code>	a list containing the parameters of the model. If specified, it overwrites the values of <code>mu</code> , <code>sigma</code> , <code>delta</code> , <code>dof</code> and <code>pro</code> .

## Details

`rmst` generates a sample `n` multivariate skew t (MST) variables. `rfmmst` generates a mixture of MST samples. Note that model parameters can be passed to `rmst` and `rfmmst` through the argument `known` or listed as individual arguments. If both methods of input were used, the parameters specified in `known` will be used.

## Value

`rmst` returns an `n` by `p` numeric matrix of generated data. `rfmmst` returns an `n` by `p+1` numeric matrix of generated data. The first `p` gives the coordinates of the generated data. The last column specifies which component each data point is generated from.

## References

- Lee S, McLachlan G (2011). On the fitting of mixtures of multivariate skew t-distributions via the EM algorithm. arXiv:1109.4706 [stat.ME]
- Lee, S. and McLachlan, G.J. (2014) Finite mixtures of multivariate skew t-distributions: some recent and new results. *Statistics and Computing*, 24, 181-202.
- Lee, S. and McLachlan, G.J. (2013) EMMIXuskew: An R package for fitting mixtures of multivariate skew t-distributions via the EM algorithm. *Journal of Statistical Software*, 55(12), 1-22. URL <http://www.jstatsoft.org/v55/i12/>.

## See Also

[dmst](#), [dfmmst](#)

## Examples

```
##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.
rfmmst(1,500, c(1,2), diag(2), c(-1,1), 4, 1)
obj <- list()
obj$mu <- list(c(17,19), c(5,22), c(6,10))
obj$sigma <- list(diag(2), matrix(c(2,0,0,1),2), matrix(c(3,7,7,24),2))
obj$delta <- list(c(3,1.5), c(5,10), c(2,0))
obj$dof <- c(1, 2, 3)
obj$pro <- c(0.25, 0.25, 0.5)
rfmmst(3, 250, obj$mu, obj$sigma, obj$delta, obj$dof, obj$pro)
rfmmst(3, 500, known=obj)
```

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