## BACHELOR FINAL PROJECT

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## Subject

Consider an abstraction of a production system. M machines numbered  $1, \ldots, M$  produce M types of products numbered  $1, \ldots, M$ . Each product undergoes two steps. Products of type i are first *created* at machine i and then moved to machine i + 1 (in case i = M then interpret i + 1 as 1). At machine i + 1, products of type i are further *processed* and then leave the system. Thus each machine (i) can perform two types of operations: *creation* of products of type i and *processing* of products of type i - 1. Products queue at the machines while waiting for their *processing* step. Thus the system contains M queues which we denote by  $X_1, \ldots, X_M$ . Queue  $X_i$  is for products of type i and is next to machine i + 1. Student: make a drawing for M = 3 to ensure you understand (bring it to the first meeting).

The machines need to divide their time between *creating* and *processing*. Assume they do so by giving preemptive priority to *processing*. This means that when ever  $X_{i-1}$  is not empty, machine *i* will work on *processing*. Otherwise, the machine will work on *creating* and will be preempted (stopped) at the instant in which  $X_{i-1}$  becomes non-empty. It is evident that the machines never idle.

A general goal is to understand under which conditions such a production system may operate in a stable manner. This may shed a light on the understanding of more complex and realistic production systems. As an approximation, assume that material (products) are a continuous quantity. Associate the positive production rates  $\lambda_i$  and  $\mu_i$  with product *i*.  $\lambda_i$  is the rate at which product *i* is *created* at machine *i*.  $\mu_i$ is the rate at which product *i* is *processed* from queue  $X_i$  at machine i + 1. Thus for example if for  $t \in [5.7, 10]$ ,  $X_i$  is not empty then  $4.3 \times \mu_i$  units of product *i* are removed from  $X_i$  during this time. Denote by  $X_i(t)$  the continuous non-negative quantity of material at queue  $X_i$  at time *t*. Further assume that the initial conditions  $\{X_i(0)\}$  are given. This fully defines the dynamics of  $\{X_i(t)\}$ .

## Assignment

(a) Create a useful computational tool (software) for generating the trajectories of  $\{X_i(t)\}$  given different parameters, M,  $\mu_i$ ,  $\lambda_i$  and initial conditions. Attempt to characterize stability (this depends on  $M, \mu_i, \lambda_i$ ).

(b) Find and implement the system of equations for production rates under the assumption of stability.

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